

# Geometry



| <b>Day</b> | <b>Topic</b>  | <b>Homework</b>  | <b>IXL</b> |
|------------|---|------------------|------------|
| 1          | Review Formulas   | Worksheet 1      | 7.AA.2     |
| 2          | Derive Volume of any Right Prism                              | Worksheet 2      | 7.AA.3     |
| 3          | Circumference of a Circle                                     | Worksheet 3      | 7.AA.7     |
| 4          | Area of a Circle  | Worksheet 4      | 7.AA.4     |
| 5          | Convert Area to Circumference and Back Again                  | Study for quiz   | 7.AA.6     |
| 6          | Quiz with Formulas  | Worksheet 5      | 7.AA.8     |
| 7          | Derive Surface Area of a Right Prism and Volume of a Cylinder | Worksheet 6      | 8.T.9      |
| 8          | Derive Volume of a Cone and a Sphere                          | Worksheet 7      | 8.T.10     |
| 9          | Practice  | Review Worksheet | 8.T.13     |
| 10         | Review  | Study for Test   |            |
| 11         | Unit Test   | none             |            |



## Day 1

Write down all of the formulas for area that you can remember and give an example of each.

Perimeter: add all sides

$$\begin{aligned} A(\text{triangle}) &= \frac{1}{2}bh \\ &= \frac{1}{2}(2)(5) \\ &= 5 \text{ cm}^2 \end{aligned}$$



?  $A(\text{circle}) = \pi r^2$

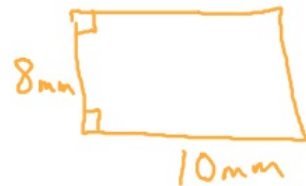
$$\begin{aligned} A(\text{square}) &= s^2 \\ &= 4^2 \\ &= 16 \text{ ft}^2 \end{aligned}$$



$$\begin{aligned} A(\text{parallelogram}) &= bh \\ &= 9(7) \\ &= 63 \text{ in}^2 \end{aligned}$$



$$\begin{aligned} A(\text{rectangle}) &= lw \\ &= 10(8) \\ &= 80 \text{ mm}^2 \end{aligned}$$



$$A(\text{trapezoid}) = \frac{1}{2}h(b_1 + b_2)$$

Half the height times the sum  
of the bases

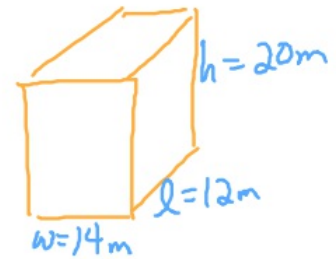
$$\begin{aligned} &\frac{1}{2}(4)(6+9) \\ &= 30 \text{ in}^2 \end{aligned}$$



$$V = lwh$$

Volume (rectangular prism)

$$\begin{aligned} V &= lwh \\ &= 12(14)(20) \\ &= 3360 \text{ m}^3 \end{aligned}$$



$$SA \text{ (rectangular prism)} = 2(lw + wh + lh)$$

OR

$$\begin{aligned} &2lw + 2wh + 2lh \\ &= 2 \cdot 12 \cdot 14 + 2 \cdot 14 \cdot 20 + 2 \cdot 12 \cdot 20 \\ &= 336 + 560 + 480 \\ &= 1376 \text{ m}^2 \end{aligned}$$

## Formulas

Perimeter of any shape: Total the distance around the shape (add all sides)

Area of a Triangle:  $A = \frac{1}{2}bh$

Area of a Square:  $A = s^2$

Area of a Rectangle:  $A = lw$

Area of a Parallelogram:  $A = bh$

Area of a Trapezoid:  $A = \frac{1}{2}h(b_1 + b_2)$

Area of a Circle:

Circumference of a Circle:

Surface Area of a  
Rectangular Prism:  $SA = 2lw + 2wh + 2lh$  or  $SA = 2(lw + wh + lh)$

Surface Area of Any  
Right Prism/Pyramid: Add the areas of all the sides

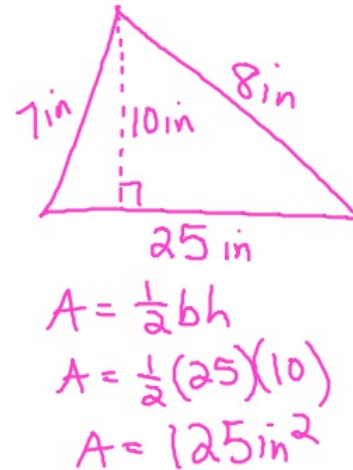
Volume of a  
Rectangular Prism:  $V = lwh$

Volume of Any  
Right Prism/Pyramid:  $V = BH$

Volume of a Cylinder:

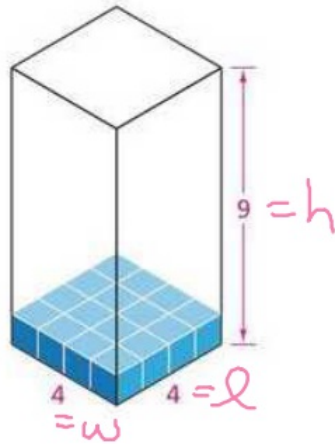
Volume of a Cone:

Volume of a Sphere:



Day 2

To calculate the exact volume of a rectangular prism, you could visualize packing it with layers of identical cubes. This works well for square prisms.

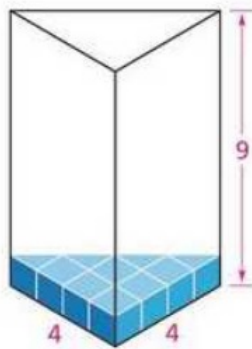


9 layers of  
16 cubes  
(4·4)

Find the volume.

$$V = lwh$$
$$V = 4(4)(9)$$
$$V = 144 \text{ unit cubes}$$

units<sup>3</sup>  
Cu. units



- How many cubes would you need to fill the prism?

72 cubes

9 layers of  
8 cubes.  
 $(A(\Delta) = \frac{1}{2}bh$   
 $= \frac{1}{2} \cdot 4 \cdot 4)$

We find that calculating the volume is the same for any right prism - no matter what the shape of the base is. Remember: by definition, a right prism has a polygonal base and rectangular lateral faces.

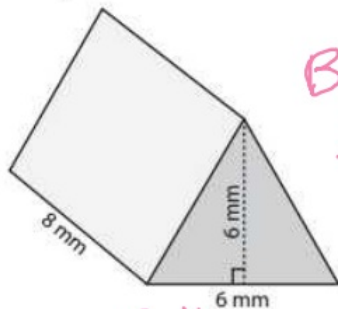
The volume for any right prism is:

$$V = BH$$

↑  
area of base

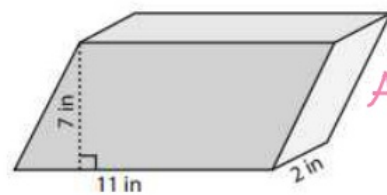
↑  
height of the prism  
(distance between the 2 bases)

Examples:



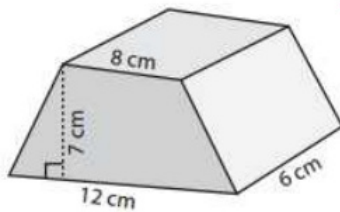
$B = \text{Area of Triangle}$   
 $A = \frac{1}{2}bh$   
 $= \frac{1}{2}(6)(6)$   
 $= 18 \text{ mm}^2$

Volume =  $\frac{BH}{1}$   
 $= 18(8)$   
 $= 144 \text{ mm}^3$



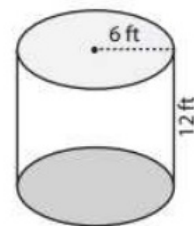
$A = bh$   
 $= 11 \cdot 7$   
 $= 77$

Volume =  $\frac{BH}{1}$   
 $= 77(2)$   
 $= 154 \text{ in}^3$



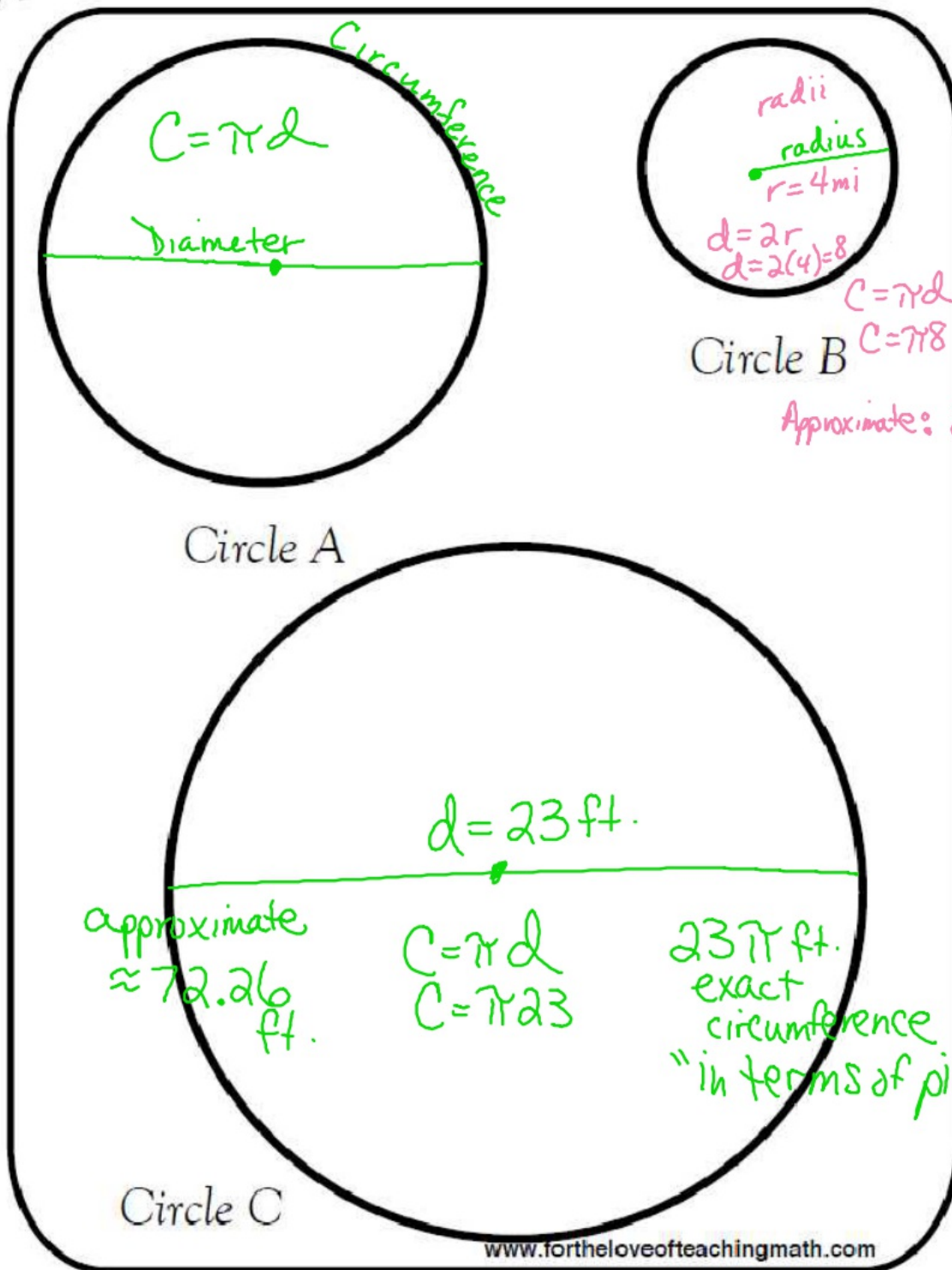
$A = \frac{1}{2}h(b_1 + b_2)$   
 $= \frac{1}{2} \cdot 7(8 + 12)$   
 $= 70$

Volume =  $\frac{BH}{1}$   
 $= 70 \cdot 6$   
 $= 420 \text{ cm}^3$



Area of the base = 113.1 sq ft

Volume =  $\frac{BH}{1}$   
 $= 113.1 \cdot 12$   
 $= 1357.2 \text{ ft}^3$



B) 1) 8km = x

$$\begin{aligned}y &= .50x + 5 \\y &= .50(8) + 5 \\y &= \$9\end{aligned}$$

2) \$10 = y

$$\begin{array}{r}10 = .50x + 5 \\-5 \qquad -5 \\ \hline 5 = .50x \\ \frac{5}{.50} \quad \frac{.50}{.50} \\ 10 = x \\ \text{km}\end{array}$$

3) (12,11)

We walked 12 km and earned \$11.

4) Alana's plan

a) table? \$5 at 0 km she earned \$5

b) graph? line starts @ 5 where her line crosses the y-axis

c) equation? added to the x → constant

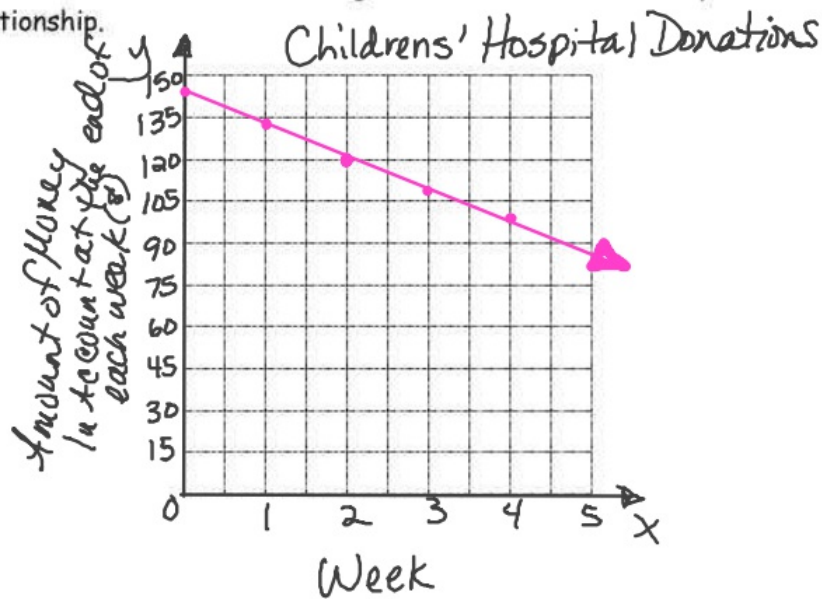


Inv 1.4

| Week | Amount of Money at the End of Each Week |
|------|---|
| 0    | 144                                     |
| 1    | 132                                     |
| 2    | 120                                     |
| 3    | 108                                     |
| 4    | 96                                      |
| 5    | 84                                      |

$2-12$        $\frac{144}{-132}$   
 $\frac{12}{12}$

- A) 1) How much money is in the account at the start of the project?  $\$144$
- 2) How much money is withdrawn from the account each week?  $\$12$
- 3) Suppose the students continue withdrawing the same amount of money each week. Sketch a graph of this relationship.



- 4) Write an equation that represents this relationship. Explain what information each number and variable represents.

$y = -12x + 144$

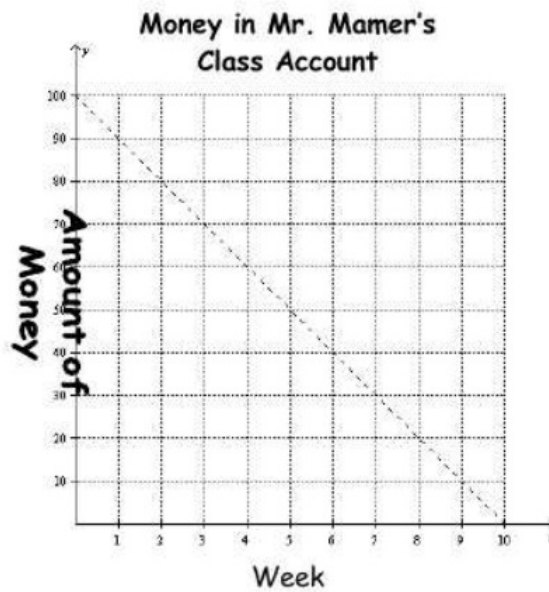
Let  $x$  = number of weeks  
 Let  $y$  = amount of money at the end of each week (\$)

$-12$ : They take \$12 out the account each week.

$144$ : The amount in the account at the start (week 0). is \$144.

5) Is the relationship between the number of weeks and the amount of money left in the account a linear relationship? Explain.

Yes, it is linear  
graph  $\rightarrow$  straight line  
table  $\rightarrow$  constant rate of change.



B) 1) What information does the graph represent about the money in Mr. Mamer's class account?

The graph tells us how much money is in the account each week.

2) Make a table of data for the first 10 weeks. Explain why the table represents a linear relationship.

| Weeks                 | 0   | 1  | 2  | 3  | 4  | 5  | 6  | 7  | 8  | 9  | 10 |
|-----------------------|-----|----|----|----|----|----|----|----|----|----|----|
| Money in Account (\$) | 100 | 90 | 80 | 70 | 60 | 50 | 40 | 30 | 20 | 10 | 0  |

3) Write an equation that represents the linear relationship. Explain what information each number and variable represents.

$$y = -10x + 100$$

Let  $x$  = number of weeks  
 Let  $y$  = money in account (\$)  
 -10: \$10 taken out of the account per week

C) 1) How can you determine if a relationship is linear from...  
 a graph?

It's a straight line

100: \$100 is what's in the account when they start (at week 0)

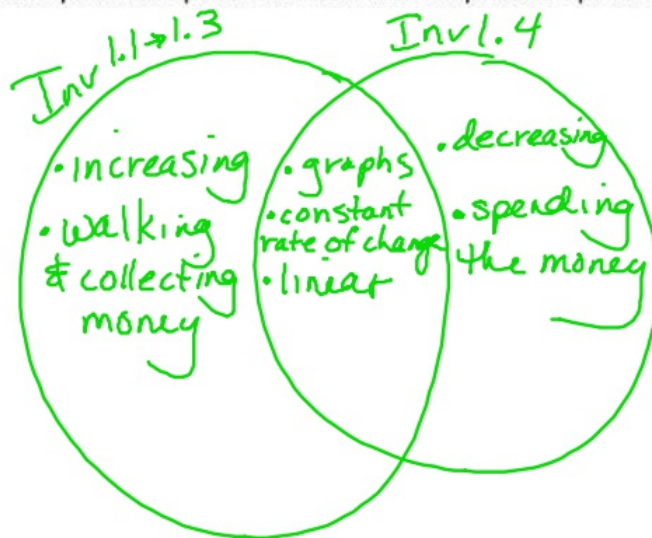
a table?

It has a constant rate of change (skip count)

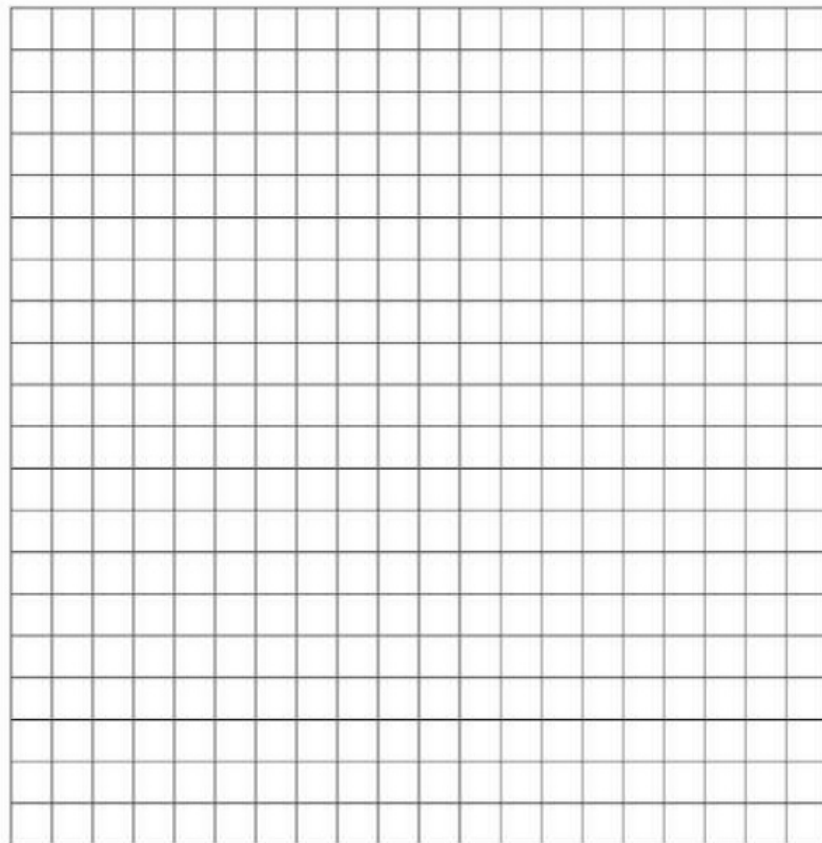
an equation?

$$y = \_x + \_$$

2) Compare the linear relationships in this problem with those in previous problems in this investigation.



Inv 2.1





Inv 2.2

A) 1)

Emile

|              |   |      |    |      |    |      |    |      |     |
|--------------|---|------|----|------|----|------|----|------|-----|
| Time (sec)   | 0 | 5    | 10 | 15   | 20 | 25   | 30 | 35   | 40  |
| Distance (m) | 0 | 12.5 | 25 | 37.5 | 50 | 62.5 | 75 | 87.5 | 100 |

Henri

|              |    |    |    |    |    |    |    |    |    |
|--------------|----|----|----|----|----|----|----|----|----|
| Time (sec)   | 0  | 5  | 10 | 15 | 20 | 25 | 30 | 35 | 40 |
| Distance (m) | 45 | 50 | 55 | 60 | 65 | 70 | 75 | 80 | 85 |

TIE

2) Graph



3) Emile:  $y = 2.5x$

Henri:  $y = x + 45$

Let  $x = \text{time (s)}$

Let  $y = \text{distance (m)}$

2.5 = Emile's walking rate (m/s)

45 = Henri's head start (45 m @ 0 s)

1 = Henri's walking rate (m/s)

0 = Emile's head start (0 m @ 0 s)

B) 1) How far does Emile walk in  $\overset{x}{20}$  seconds?  $50\text{ m}$

$y = 2.5x$   
 $y = \frac{2.5\text{ m}}{\text{s}} \cdot 20\text{ s}$   
 $y = 50\text{ m}$

2) After 20 seconds, how far apart are the brothers?  
*Henri*  $\rightarrow 65\text{ m}$        $65\text{ m} - 50\text{ m} = 15\text{ m}$

3) Is the point (26, 70) on either graph? Explain.  
 $y = x + 45$   
 $70 = 26 + 45$   
 $70 \neq 71$       This point is not on either line.

4) When will Emile overtake Henri? Explain.  
 Emile and Henri will tie at 30 seconds and 75 meters. After that Emile will be winning.

C) 1) How can you determine which of two lines will be steeper from a table?  
 The constant rate of change (skip count) will be higher in the table of the steeper line.

2) How can you determine which of two lines will be steeper from an equation?  
 The coefficient of  $x$  will be bigger.

D) 1) At what points do Emile's and Henri's graphs cross the y-axis?

Emile:  $(0, 0)$   
 Henri:  $(0, 45)$        $x = 0$

2) What information do these points represent in terms of the race?

3) How can these points be found in a table?

How can these points be found in an equation?

Inv 2.3

$m = \frac{\Delta y}{\Delta x} = \frac{\text{rise}}{\text{run}}$  → "the change in" → Slope per Coefficient multiplied by x  
 Skipcount / Constant rate of change  
 Steepness

$y = mx + b$   
 $m$  → Slope per Coefficient multiplied by x  
 $b$  → y-intercept → the point where the line crosses the y-axis  
 no matter what (starting amount when  $x=0$ )  
 constant added to x  
 y value when  $x=0$   
 beginning amount

$C_{\text{MIGHTY}} = 49 + n$

$C_{\text{NOSHINK}} = 4.5n$

A) 1) For each equation, explain what information the y-intercept and the coefficient (slope) of n represent.

$m = 1$  costs \$1 per shirt  
 $b = 49$  pay \$49 for 0 shirts (up front fee)

$m = 4.5$  \$4.50 per shirt  
 $b = 0$  \$0 up front fee

2) 12 T-shirts? = n

$C_M = 49 + n$   
 $C_M = 49 + 12$   
 $C_M = \$61$

$C_N = 4.5n$   
 $C_N = 4.5(12)$   
 $C_N = \$54$

20 T-shirts?

$C_M = 49 + n$   
 $= 49 + 20$   
 $= \$69$

$C_N = 4.5n$   
 $= 4.5(20)$   
 $= \$90$

3) Lani calculates that the school has about \$120 to spend on T-shirts. From which company will \$120 buy the most shirts?  $C = \$120$

$C_M = 49 + n$   
 $120 = 49 + n$   
 $-49 \quad -49$   


---

 $71 = n$   
 + shirts

$C_N = 4.5n$   
 $120 = 4.5n$   
 $\frac{120}{4.5} \quad \frac{4.5}{4.5}$   


---

 $26.\bar{6} = n$   
 $26 \text{ shirts}$



4) a) For what number of T-shirts is the cost of the two companies equal? What is the cost?

$$C_M = 49 + 14n$$

$$= \$63$$

$$C_N = 4.5(14)$$

$$= \boxed{\$63}$$

$$C_M = C_N$$

$$49 + n = 4.5n$$

$$\frac{49}{3.5} = \frac{3.5n}{3.5}$$

$$n = 14 \text{ shirts}$$

b) How can this information be used to decide which plan to choose?

If they buy less than 14 shirts, they should buy from No Shrink. If more, they should buy from Mighty.

5) Explain why the relationship between the cost and the number of T-shirts for each company is a linear relationship.

They are linear because they have a constant rate of change.  
(you pay one price per shirt)

B) The table below represents the costs from another company, The Big T.

|   |    |      |    |      |    |      |    |      |    |      |    |
|---|----|------|----|------|----|------|----|------|----|------|----|
| n | 0  | 1    | 2  | 3    | 4  | 5    | 6  | 7    | 8  | 9    | 10 |
| C | 34 | 36.5 | 39 | 41.5 | 44 | 46.5 | 49 | 51.5 | 54 | 56.5 | 59 |

$$m = \frac{\Delta y}{\Delta x} = \frac{5}{2} = 2.5$$

1) Compare the costs for this company with the costs for the two companies in Question A.

\$2.50 per shirt  
\$34 set up fee (cost for 0 shirts)

2) Does this plan represent a linear relationship? Explain.

This is linear because it has a constant rate of change.

3) a) Could the point (20, 84) lie on the graph of this cost plan? Explain.

$$C_T = 2.5n + 34$$

$$84 = 2.5(20) + 34$$

$$84 = 50 + 34$$

$$84 = 84 \checkmark$$

This point will be on the graph.